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Advice:

Get papers back from TAs.

‘Best’ labs posted across hall from 111 labs in glass case each week. No labs accepted after solution posted. Anyone objecting to having their labs posted – let me know via email.

Today: lec 4 Diodes
lec 5 TH Feb 1
lec 6 TH Feb 8
lec 7 TH Feb 15

Utility of following discussion:

Complaints about not enough solid state detail \Rightarrow small signal models not well motivated.

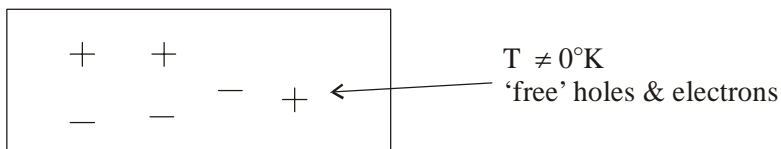
I will give some detail, but you promise to remember:

good design \Rightarrow circuit NOT sensitive to details of device parameters

Instruments & Devices:

Semiconductor Diode

Pure semiconductor: covalent bonds, (all 4 valence electrons used), 1.1 eV band gap (silicon)
 \Rightarrow thermal excitations important



$\approx 10^{10}$ carriers/cm³ for Si @ 300°K ($\sim 10^{23}$ for metal)
 \Rightarrow semiconductor

Doping

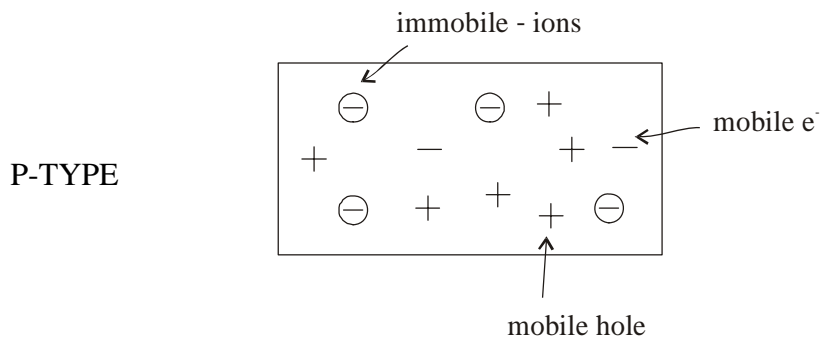
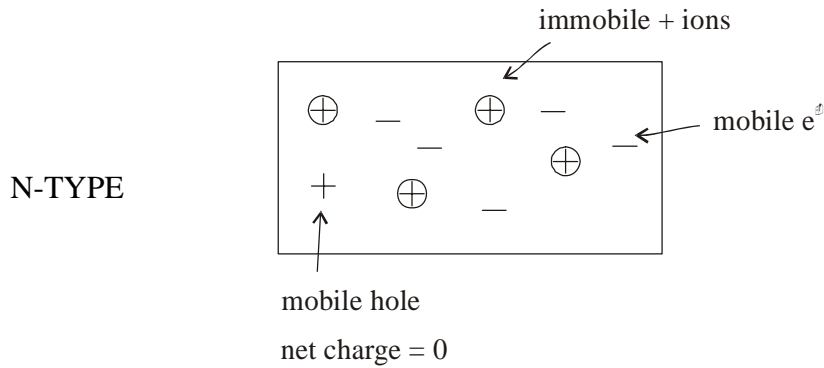
Add impurities to control the e-hole balance.

5 valence electrons \Rightarrow extra electron gets loose (donor)

3 valence electrons \Rightarrow extra hole gets loose (acceptor)

- Donor – phosphorus, arsenic, antimony
electrons majority carrier, holes minority carrier \equiv n-type

- Acceptor – boron, gallium, aluminum, indium
holes majority carrier, electrons minority carrier \equiv p-type



10^{15} carriers $\Rightarrow \approx 10^{15}$ donor atoms/cm³

Si has $\sim 5 \times 10^{22}$ atoms/cm³ \Rightarrow 1 impurity/50 x 10⁶ Si

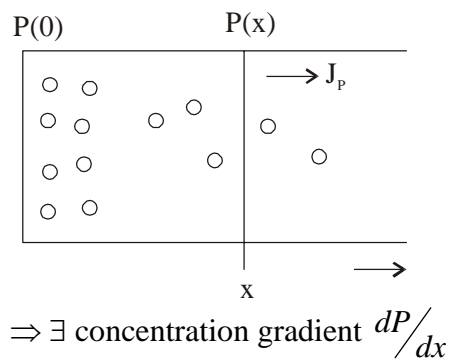
20 μ g of phosphorus/kg SI \Rightarrow extreme care in manufacture

Application of a voltage causes a drift of charge, carried by both holes & electrons. Total current is the sum of the 2 currents.

* As in a metal, but 2 carriers

Diffusion Current

Suppose concentration of holes varies with position:



Density of holes on one side of surface > on the other. Because of random thermal motion, they want to drift toward lower concentration region. This current is proportional to the concentration gradient:

$$J_p = -qD_p \frac{dP}{dx} \quad D_p = \text{diffusion constant for holes}$$

$$\left(\frac{dP}{dx} < 0, J_p > 0 \text{ in } +x \text{ direction} \right)$$

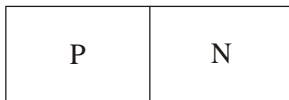
An electric field will be set up within the Si block to hold the equilibrium current to zero.
 * Very different from metal

NB: Drift current density under influence of \vec{E} given by $\vec{J}_{drift} = q(p\mu_p + n\mu_n)\vec{E}$

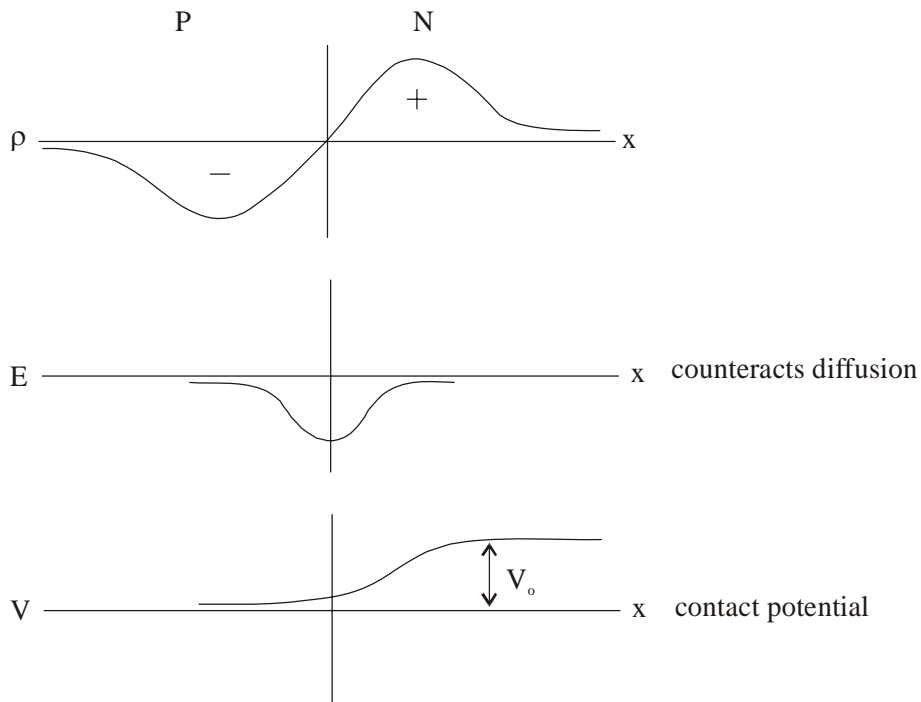
p/n = hole/electron density

μ_p/μ_n = hole/electron mobility

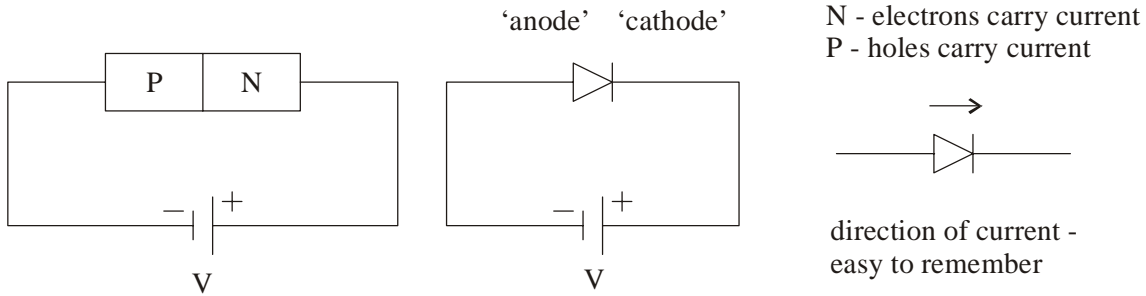
P-N Junction



Electrons & holes diffuse both ways \Rightarrow depletion region (0.5 μm thick) is generated (or space charge layer)



Reverse Bias



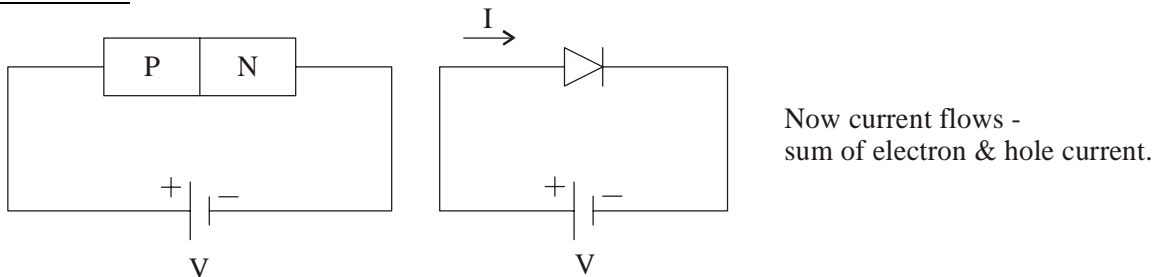
This polarity causes holes & electrons to move away from the junction.

≈ 0 current (some current because thermal e-hole generation. Holes anywhere on n side drift to gap & are then pulled by the field).

= reverse saturation current $\equiv I_S$ (\approx independent of V , depends on T)

(N.B. Addition of minority carriers (T, \dots) inferences this i_{sat} – important for transistor operation)

Forward Bias



Contacts metal – semiconductors are ohmic, voltage drop across crystal (ideally) 0, then applied V appears to add to junction potential.

- Time varying signals: charge goes into/out of space charge layer \Rightarrow looks like a capacitance \equiv transition capacitance C_T , function of reverse voltage. ($10 \rightarrow 200$ pF). Important for transistor operation
- Field is reduced in the space-charge layer, allows majority carriers to diffuse across the junction to the side where they are in the minority (injection of minority carriers).
- Time varying signals: diffusion, or storage capacitance C_D (more later). $C_D \gg C_T \sim 10 \mu\text{F}$ (however, $rC_D = \tau \sim \text{nsec}$, so time constant is small)

Diode behavior in both regions described by ('exponential diode')

$$I = I_s \left(e^{qV/kT} - 1 \right)$$

$q = \text{electron charge } e$

$k = \text{boltzmann's constant } 1.38 \times 10^{-23} \text{ J / } ^\circ\text{K}$

$T = ^\circ\text{K}$

$$\frac{kT}{q} = 26 \text{ mV @ } 300 \text{ K}$$

$$V \gg \frac{kT}{q} \Rightarrow \text{neglect (1)}$$

$$\text{Forward bias} \Rightarrow I = I_s e^{qV/kT} \gg I_s$$

$$\text{Reverse bias} \Rightarrow V \ll \frac{kT}{q} \Rightarrow i = -I_s$$

Silicon: $I_s \sim 10 \text{ pA}$

$$\ln\left(\frac{I}{I_s}\right) = \ln\left(e^{qV/kT} - 1\right)$$

$$\ln\left(\frac{I}{I_s}\right) \approx \frac{qV}{kT}$$

$$V = \frac{kT}{q} \ln\left(\frac{I}{I_s}\right) \quad (I_s \sim 10 \text{ pA})$$

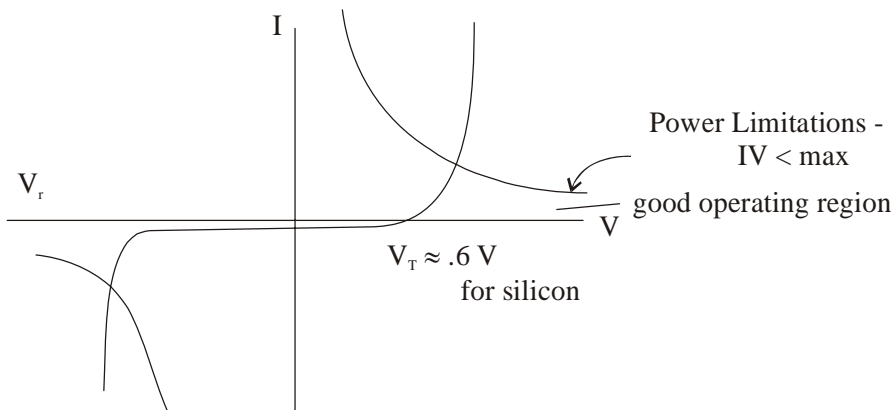
$$V(I = 20 \text{ mA}) \sim 26 \text{ mV} \ln\left(\frac{20 \text{ mA}}{10 \text{ pA}}\right)$$

$$\sim .56 \text{ V} \equiv V_T$$

on $\Rightarrow \sim 0.6 \text{ V drop}$

off $\Rightarrow \text{open}$

Real Diode Characteristics:

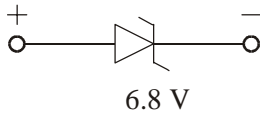


High forward currents: ohmic contacts take over & diode behaves as a resistor.

High reverse voltages: minority carriers gain sufficient speed to knock loose additional electrons (in depletion region where field is high) \Rightarrow larger reverse current – avalanche multiplication

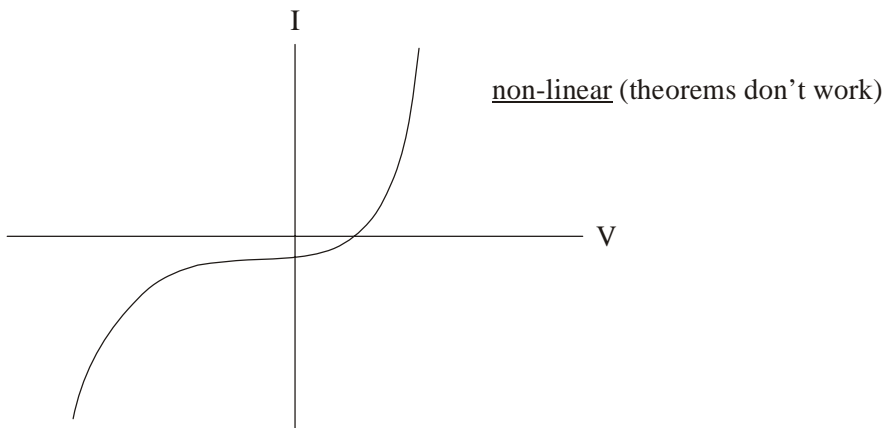
Maximum reverse voltage $V_R \equiv$ maximum reverse blocking voltage.

Zeners have a well controlled V_R (independent of i), can be used as a voltage references

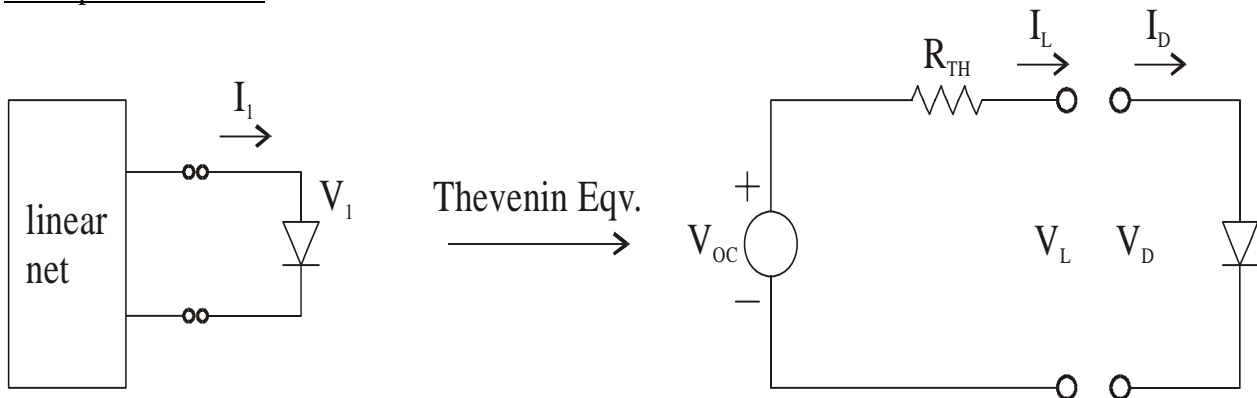


Instruments & Devices + Circuit Analyses

Diodes as Network Elements



I. Graphical Method



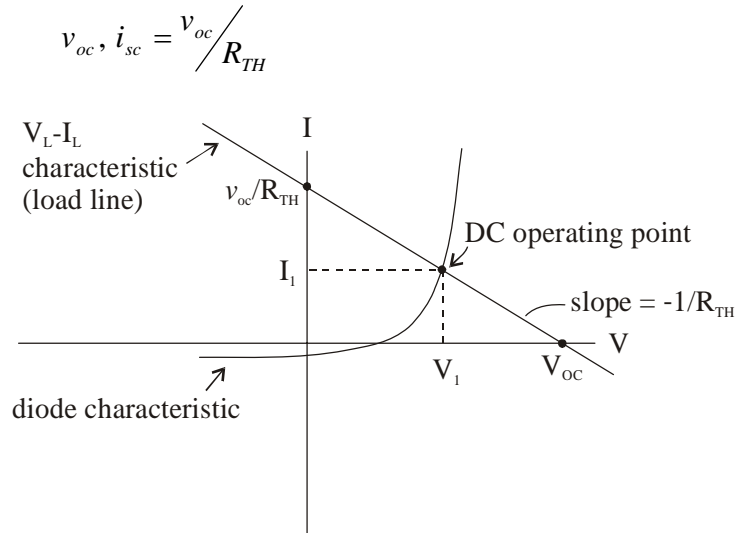
If we can find I_1 , V_1 , we are done.

We know V_D vs. I_D from characteristic curve (manufacturer's or measured)

We know $V_L = V_{OC} - I_L R_{TH}$

Plot this on the i - v characteristic line.

2 points = open circuit voltage & short-circuit current

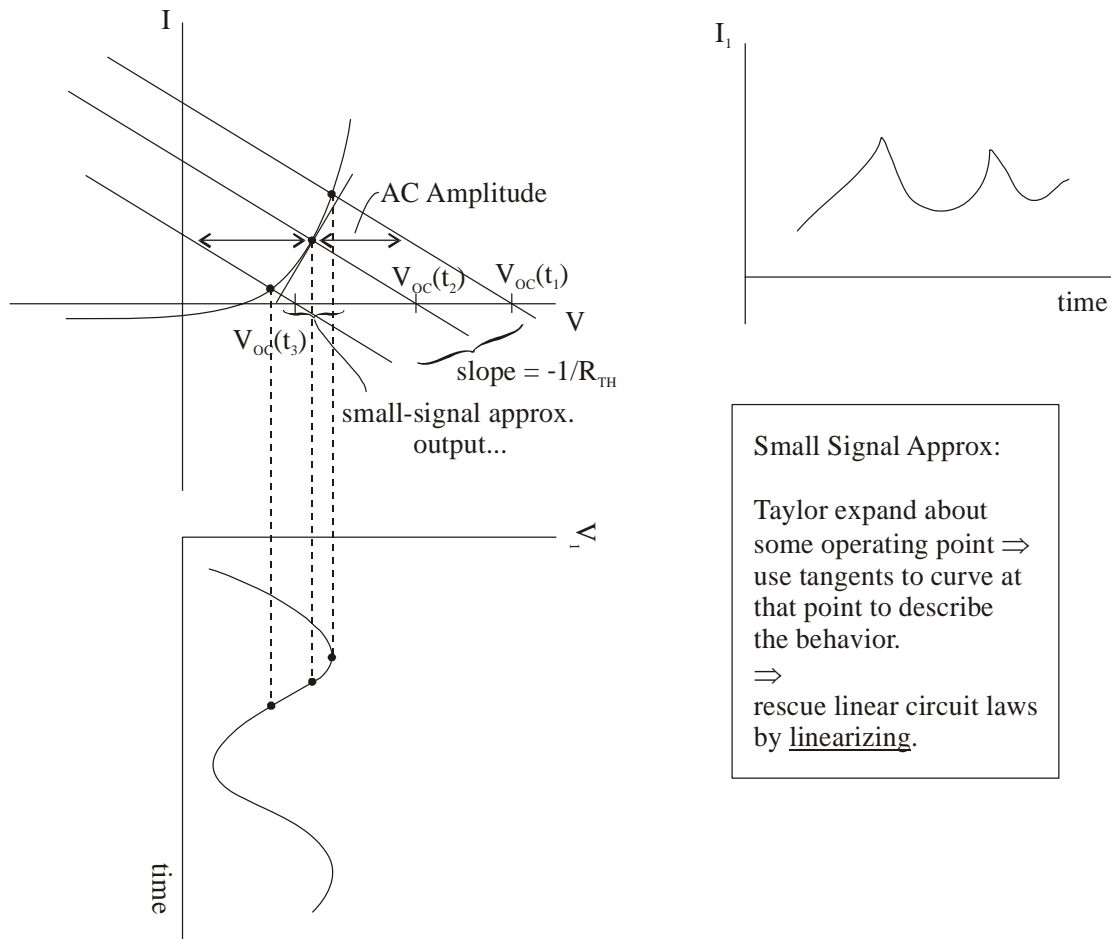


see example page 157 S&S

Source is time varying: (see page 164 S&S)

R_{TH} remains constant, V_{OC} varies

\Rightarrow Load line has constant slope $\left(-\frac{1}{R_{TH}}\right)$, but the intercept (V_{OC}) moves as a function of time, so the operating point moves:

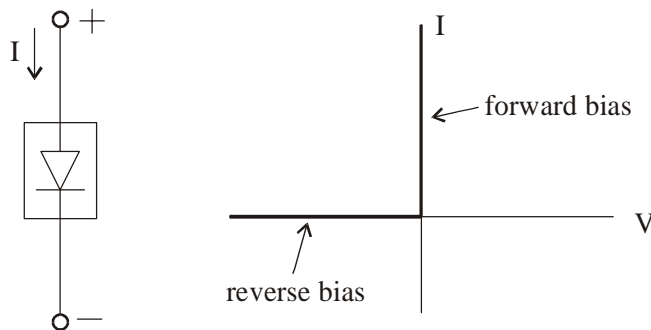


II. Linearize (the behavior for small deviations about the operating point.)

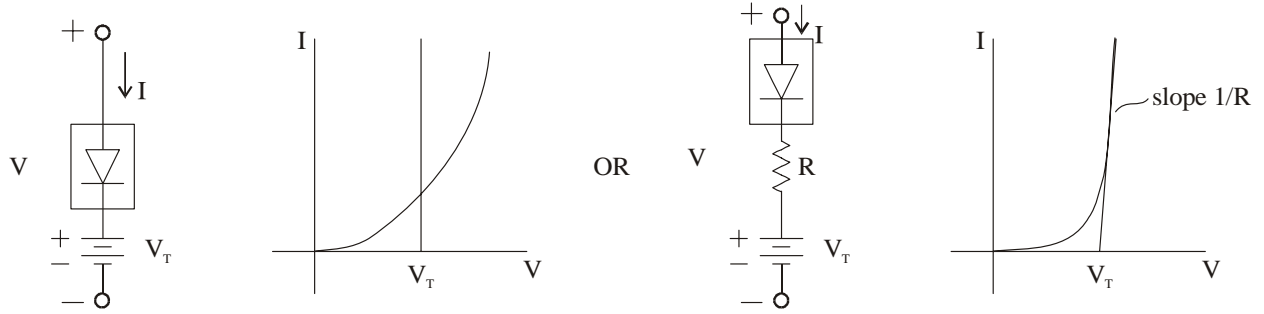
\Rightarrow Taylor expand, keep 1st term. **N.B. doesn't work over whole range!**

Approximate diode behavior with linear elements over limited i - v range.

Ideal diode: (switch)



If voltages not large compared to .6 V, then:



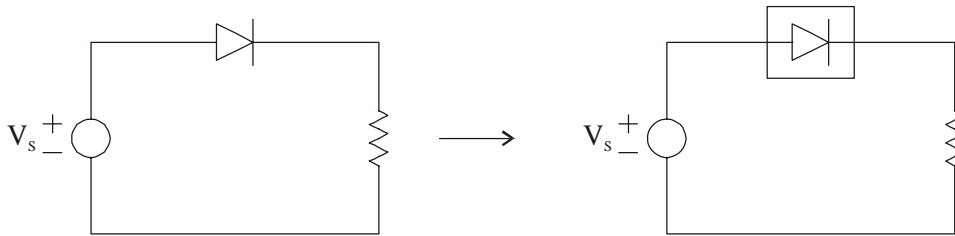
Reverse current zero usually ok.

Use simplest model to meet your needs!

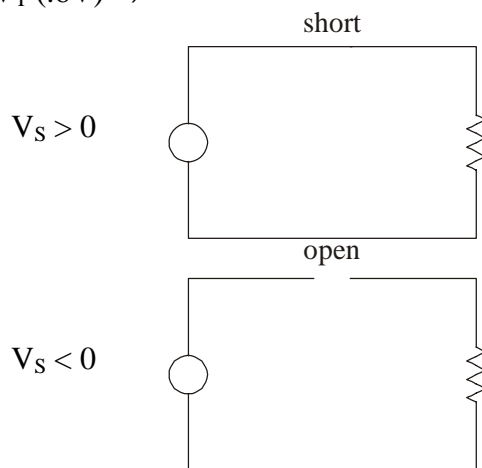
Circuit Analyses

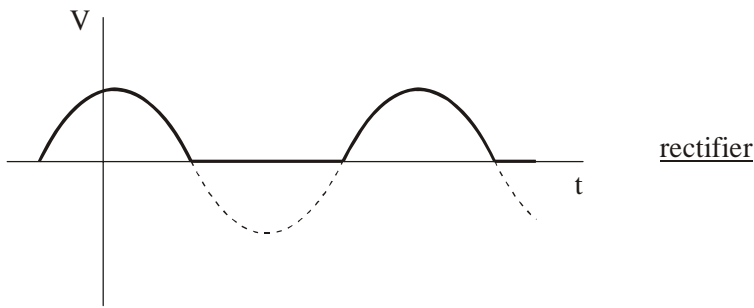
Examples:

Rectification:



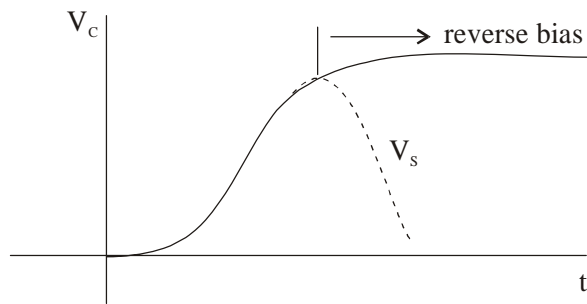
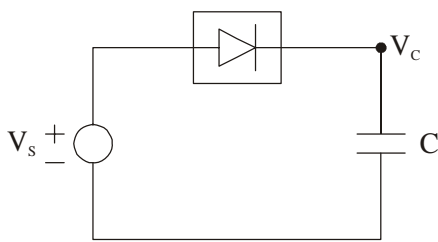
$V_s \gg V_T (.6V) \Rightarrow$





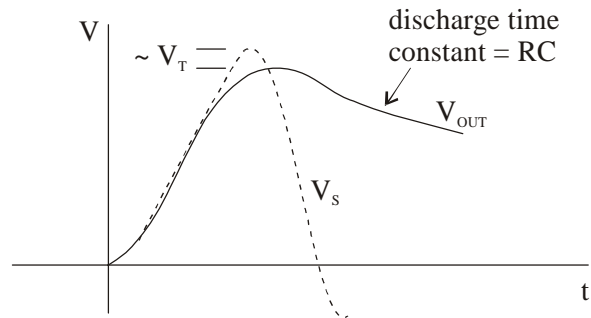
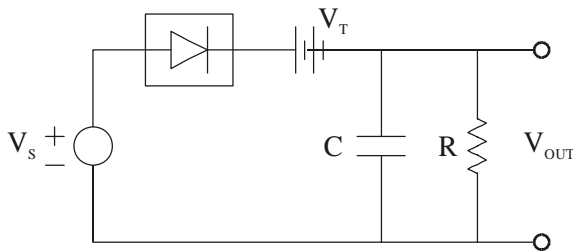
Another example: matched pairs pg. 49 H&H

Peak Sampler



- V_s gives positive, diode a short.
- Past V_s max, diode is reverse biased & we are stuck.

More realistic:



Amount that it drops depends on frequency of V_s & RC time constant (NB – RC comes from step response).

LEDs

Same as ordinary diodes, but forward voltage drop in range 1.5 – 2.5 V, 5 – 20 mA of current causes light to be emitted. (electron-hole recombination)

Inverse also works – reverse-biased diode can be light-sensitive (photodiode). Important for ‘electric eyes’. Also, basis for light & particle detection - liberate e-h pairs within depletion region.

Summary

Reverse bias = open

Forward bias = closed

(>0.6V) = .6V drop = good diode model for most uses